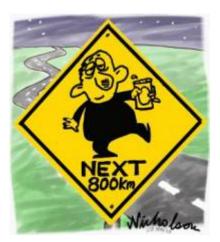
• Kanda

# Random walks: the drunk and the canyon -Tutorial for EcoVirtual



Imagine that a drunkard is walking in a huge plains, that has a canyon on one of the sides. Every time the drunkard steps forward, he also staggers to the left or to the right, with equal probability.

This is a very simple Markovian process, called random walk, on one dimension<sup>1)</sup>. When the drunkard falls in the canyon, the random walk is over (and so is the drunkard), so we call this condition as *absorbing boundary*.

# Virtual drunks

To proceed, you must have the R environment with the Remdr and Ecovirtual packages installed and loaded. If you do not have and do not know how to have them, see the Installation page.

What can we predict about this process? Let's set some drunks lose on this virtual plains. To do this, we will use the menu **EcoVirtual > Biogeographical Models > Random Walk** to open the following options window:

Last update: 2017/09/19 17:16	en:ecovirt:roteiro:math:bebadorcmdr http://ecovirtual.ib.usp.br/doku.php?id=en:ecovirt:roteiro:math:bebadorcmdr
----------------------------------	---

000	RCon	nmander								
Arquivo	Editar	Dados	Estatísticas	Gráficos	Modelos	Distribuições	EcoVirtual Fe	rramentas Ajuda		
P <sub>o r</sub>	andon V	Valk Sim	ulation			Editar o	onjunto de dado	s Ver conjunto de dados	Modelo:	<sem modelo<="" th=""></sem>
Rando	n Walk I Nur	Paramete nber of S Ste initial dis il distanc	ata set: Do_N ens pecies 10 psize 1 stance 200 e equal 1000	]			= FALSE) = FALSE) = TRUE)			
	ок	0	Cancelar		Ajuda					Subm
> sinH > rand > rand	ubl(5 = Nalk(n Nalk(n	10, j - 10, s - 10, s	tep = 1, c:	o = 1000) iclo = 1e iclo = 1e	+05, x1m +05, x1m	Ax =200, all: ax =200, all: ax =200, all:	rq = FALSE)			
[4] ER	RO: ob		" não encor " não encor							

Simulation parameters:

Option	Parameter	
Number of Species	S	Number of drunks
Step Size	ISIAN	Number of steps the drunk moves sideway at each time interval
Maximum Initial Distance	xlmax	maximum distance between the drunks and the canyon when the simulation starts
Initial Distance Equal	alleq=TRUE	when selected (TRUE), all drunks start at the maximum distance. When unselected, the drunks start at random position from 1 to the maximum distance above
Maximum time	tmax	total simulation time

#### Example

Let's simulate ten drunkards, staggering for 10 steps at each time interval, for ten thousand time steps:

S =10
step = 10
xlmax = 200
alleq = TRUE
tmax = 10000

As with every stochastic process, the results may vary at each simulation. Thus, repeat the simulation some times to make sure you understand the results.

#### Step effect

2022/12/21 20:18

3/5

What happens if the drunks are more or less staggering? Try reducing the step size to 2:

S = 10
step = 2
xlmax = 200
alleq = TRUE
tmax = 10000

#### **Time effect**

Drunks that stagger less are less prone to end in the bottom of the canyon, or is it only a matter of time? Try increasing the final time:

S = 10
step = 2
xlmax = 200
alleq = TRUE
tmax = 50000

#### Question

The drunk has equal probability to stagger left or right, so on the average he only walks forward. Given enough time, this random walk with absorbing boundary has only one possible outcome. What is it?

## **Virtual population**

To simulate this dynamics, open the **EcoVirtual > One population > Demographic Stochasticity** window:

🔹 🏟 Demographic Stochasticity					
Enter name fo	Do_Not_Sa	ve			
Maxi	50		•		
Number of s	20				
Population paramete					
	100				
	0.2				
C	0.2				
🔞 Ajuda	<b>X</b> C	Cancelar	🚽 OK		

The options here control the simulation of populations under a continuous time random walk:

Option	Parameter	Definition
Enter name for last simulation data set	R object	R object in which to save the simulation results
Maximum time	tmax	Maximum simulation time, in the same time unit as the rates used
Number of simulations	nsim	Number of different populations to simulate
Initial size	N0	Initial population size
birth rate	b	instantaneous birth rate (\$b\$)
death rate	d	instantaneous death rate (\$d\$)

#### Example

Simulate the trajectory of 20 population with equal birth and death rates, starting with 10 individuals each. Let the time continue up to 50 units:

tmax = 50 nsim = 20 N0 = 10 b = 0.2d = 0.2

You should see a random walk graph, very similar to the drunks. The number of extinctions up to the Maximum time is recorded in the upper left corner of the graph.

#### Questions

- 1. Which are the corresponding parameters between the drunk random walk and the birth and death dynamics?
- 2. The effects you have noted on the drunk simulation (step size and end time) affect the population dynamics in the same way?
- 3. What is the consequence of this result for the conservation of natural populations?

### To learn more

- We have simulated a dynamic with equal probability of births and deaths with an absorbing boundary. This is a particular case of stochastic birth and death processes. You can read more about them in the tutorial on demographic stochasticity.
- Chemotaxis How a Small Organism Finds a Food Source: one excellent explanation about random walk and its application to another area in biology, as presented by MIT students.

1)

we are only interested in the lateral movement

×

From: http://ecovirtual.ib.usp.br/ -

Permanent link: http://ecovirtual.ib.usp.br/doku.php?id=en:ecovirt:roteiro:math:bebadorcmdr

Last update: 2017/09/19 17:16